## HHHS MATH DEPARTMENT AD CALCULUS SUMMER DRED DACKET

Welcome to AP Calculus! This summer review packet includes prerequisite topics from algebra, trigonometry, and geometry that are necessary for success in calculus. You will be given an opportunity to ask questions on these topics in September.

Instructions:

- Complete the entire packet neatly on loose-leaf (or unlined paper), showing all work. Clearly number each problem.
- Check your answers and retry problems until you have mastered the contents of this packet.
- This will be collected the first day of school for a weighted homework grade. You will also be assessed on your mastery of these topics in the second week of school (following the first Wednesday after-school extra-help session).

**Contents:** 

- 108 Practice Questions and Answers
- 29 Additional Trigonometry Practice Problems [You must be able to do these without having to draw (or refer to) a full unit circle. You should be able to answer them in your head with possibly a rough sketch of the particular radian measure.]
- Worked-out solutions to the problems with review tips.

# In addition to the worked-out solutions, the following are helpful resources if you need assistance with a topic.

https://www.khanacademy.org/

http://www.wyzant.com/resources/lessons/math/precalculus http://www.slader.com/subject/math/precalculus/homework-help-andanswers/

Or google search each topic as you have trouble.

My email: cassanop@hhschools.org

AP Calculus AB Summer Review Packet

Simplify

1. 
$$\frac{x^3 - 9x}{x^2 - 7x + 12}$$
  
2.  $\frac{x^2 - 2x - 8}{x^3 + x^2 - 2x}$   
3.  $\frac{\frac{1}{x} - \frac{1}{5}}{\frac{1}{x^2} - \frac{1}{25}}$   
4.  $\frac{9 - x^{-2}}{3 - x^{-1}}$ 

Rationalize the denominator

5. 
$$\frac{2}{\sqrt{3}+\sqrt{2}}$$
 6.  $\frac{4}{1-\sqrt{5}}$  7.  $\frac{1-\sqrt{5}}{1+\sqrt{3}}$ 

Write each of the following expressions in the form of  $ca^pb^q$  where c, p, and q are numbers

8. 
$$\frac{(2a^2)^3}{b}$$
  
9.  $\sqrt{9ab^3}$   
10.  $\frac{a(2/b)}{3/a}$   
11.  $\frac{ab-a}{b^2-b}$   
12.  $\frac{a^{-1}}{(b^{-1})\sqrt{a}}$   
13.  $\left(\frac{a^{2/3}}{b^{1/2}}\right)^2 \left(\frac{b^{3/2}}{a^{1/2}}\right)$ 

Solve for x. Do not use a calculator

14. 
$$5^{(x+1)} = 25$$
16.  $\log_2 x = 3$ 15.  $\frac{1}{3} = 3^{2x+2}$ 17.  $\log_3 x^2 = 2\log_3 4 - 4\log_3 5$ 

Simplify

18. 
$$\log_2 5 + \log_2 (x^2 - 1) - \log_2 (x - 1)$$
  
19.  $2 \log_4 9 - \log_2 3$   
20.  $3^{2 \log_3 5}$ 

Simplify

21. 
$$\log_{10} 10^{1/2}$$
  
23.  $2 \log_{10} \sqrt{x} + 3 \log_{10} x^{1/3}$   
24.  $\log_{10} \frac{1}{10^{x}}$ 

Solve the following equations for the indicated variable

24. 
$$\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$$
, for a  
25.  $V = 2(ab + bc + ca)$ , for a  
26.  $A = 2\pi r^2 + 2\pi rh$ , for positive h  
27.  $A = P + \pi rP$ , for P  
28.  $2x - 2yd = y + xd$ , for d  
29.  $\frac{2x}{4\pi} + \frac{1-x}{2} = 0$ , for x

For each equation complete the square and reduce to one of the standard forms  $y - y_1 = A(x - x_1)^2$  or  $x - x_1 = (y - y_1)^2$ 

$$30. y = x^{2} + 4x + 3$$
$$32. 9y^{2} - 6y - 9 - x = 0$$
$$31. 3x^{2} + 3x + 2y = 0$$

Factor completely

$$33. x^6 - 16x^4$$
 $35. 8x^3 + 27$  $34. 4x^3 - 8x^2 - 25x + 50$  $36. x^4 - 1$ 

Find all real solutions

$$37. x^{6} - 16x^{4} = 0$$

$$39. 8x^{3} + 27 = 0$$

$$38. 4x^{3} - 8x^{2} - 25x + 50 = 0$$

Solve for x

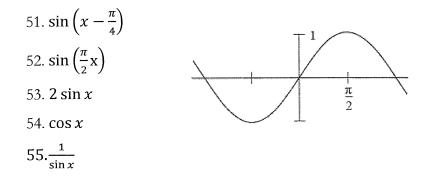
40.  $3\sin^2 x = \cos^2 x;$   $0 \le x < 2\pi$ 41.  $\cos^2 x - \sin^2 x = \sin x; -\pi < x \le \pi$ 42.  $\tan x + \sec x = 2\cos x; -\infty < x < \infty$ 

Without using a calculator, evaluate the following:

43. cos 210°	46. $\sin^{-1}(-1)$
44. $\sin\frac{5\pi}{4}$	47. $\cos \frac{9\pi}{4}$
45. $\tan^{-1}(-1)$	48. $\sin^{-1}\left(\frac{\sqrt{3}}{2}\right)$

49. 
$$\tan\left(\frac{7\pi}{6}\right)$$
  
50.  $\cos^{-1}\left(\sin\left(-\frac{\pi}{4}\right)\right)$ 

Given the graph of  $y = \sin x$ , sketch the graphs of:



Solve the equations

56. 
$$4x^2 + 12x + 3 = 0$$
  
57.  $2x + 1 = \frac{5}{x+2}$   
58.  $\frac{x+1}{x} - \frac{x}{x+1} = 0$ 

Find the remainders on division of

59.  $x^5 - 4x^4 + x^3 - 7x + 1$  by x + 260.  $x^5 - x^4 + x^3 + 2x^2 - x + 4$  by  $x^3 + 1$ 61. The equation  $12x^3 - 23x^2 - 3x + 2 = 0$  has a solution x = 2. Find all other solutions. 62. Solve for x, the equation  $12x^3 + 8x^2 - x - 1 = 0$  (all solutions are rational and between  $\pm 1$ ) Solve the inequalities. Give the solution in interval notation

$$63. x^2 + 2x - 3 \le 0 \qquad \qquad 64. \frac{2x - 1}{3x - 2} \le 1 \qquad \qquad 65. \frac{2}{2x + 3} > \frac{2}{x - 5}$$

Solve for x. Give the solution in interval notation

$$66. |-x+4| \le 1 \qquad \qquad 67. |5x-2| = 8 \qquad \qquad 68. |2x+1| > 3$$

Determine the equation of the following lines

69. The line through (-1, 3) and (2, -4)

70. The line through (-1, 2) and perpendicular to the line 2x - 3y + 5 = 0

71. The line through (2,3) and the midpoint of the line segment from (-1,4) to (3,2)

72. Find the point of intersection of the lines: 3x - y - 7 = 0 and x + 5y + 3 = 0

73. Shade the region in the xy-plane that is described by the inequalities  $\begin{cases} 3x - y - 7 < 0\\ x + 5y + 3 \ge 0 \end{cases}$ 

Find the equations of the following circles:

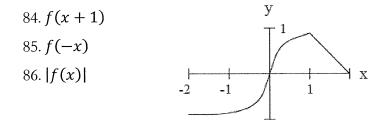
- 74. The circle with center at (1, 2) that passes through the point (-2, -1)
- 75. The circle that passes through the origin and has intercepts equal to 1 and 2 on the x and y axes respectively.
- 76. For the circle  $x^2 + y^2 + 6x 4y + 3 = 0$  find the center and the radius
- 77. Find the domain of  $\frac{3x+1}{\sqrt{x^2+x-2}}$

Find the domain and range of:

78. 
$$f(x) = 7$$
 79.  $g(x) = \frac{5x-3}{2x+1}$  80.  $f(x) = \frac{|x|}{x}$ 

Simplify 
$$\frac{f(x+h)-f(x)}{h}$$
 when  
81.  $f(x) = 2x + 3$   
82.  $f(x) = \frac{1}{x+1}$   
83.  $f(x) = 3x^2 - x + 5$ 

The graph of the functions y = f(x) is given as follows: Determine the graphs of the functions:



Sketch the graphs of the functions

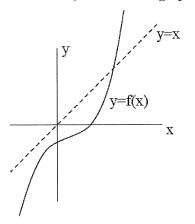
87. g(x) = |3x + 2|88. h(x) = |x(x - 1)|

- 89. The graph of a quadratic function has x-intercepts −1 and 3 and a range consisting of all numbers less than or equal to 4. Determine an expression for the function.
- 90. Sketch the graph of the quadratic function  $y = 2x^2 4x + 3$

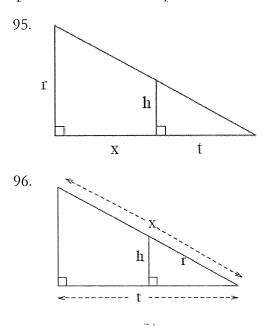
Find the inverse of the functions

91. f(x) = 2x + 392.  $f(x) = \frac{x+2}{5x-1}$ 93.  $f(x) = x^2 - 2x - 1, x > 0$ 

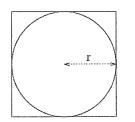
94. A function f(x) has the graph below. Sketch the graph of the inverse function  $f^{-1}(x)$ .



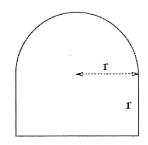
For problems 96 and 97, express x in terms of the other variables in the picture:



97. Find the ration of the area inside the square but outside the circle to the area of the square in the picture below



98. Find the formula for the perimeter of the window of the shape in the picture below



- 99. A water tank has the shape of a cone (like an ice cream cone without the ice cream). The tank is 10m high and has a radius of 3 m as the top. If the water is 5 m deep (in the middle) what is the surface area of the top of the water?
- 100. Two cars start moving from the same point. One travels south at 100 km/hr, the other west at 50 km/hr. How far apart are they two hours later?
- 101. A kite is 100 *m* above the ground. If there are 200 *m* of string out, what is the angle between the sting and the horizontal. (Assume that the string is perfectly straight.)

If 
$$f(x) = 2x - 3$$
 and  $g(x) = \sqrt{3x - 1}$ , Find:

102. 
$$f(g(x))$$

103. g(f(x))

104. If 
$$f(x) = \frac{3}{x}$$
 and  $g(x) = \frac{x}{2x-1}$ , Find  $f(g(x))$  and state its domain.

Decompose each composition function into individual function. (If y = f(u), identify u and rewrite y in terms of u)

105.  $y = \sin 3x$  107.  $y = (x^2 - 2x + 5)^5$ 

106. 
$$y = \sqrt[5]{2x+1}$$
 108.  $y = \cos^2 x$ 

### ······

1. INSTRUCTIONS: Answer each of the following without a calculator taking no longer than 20 seconds per question. Answers must be exact (no decimals) and radicals need to be simplified/rationalized.

 $\sin\frac{2\pi}{3} =$ 

Name:

**AP Calculus** 

- 2.  $\sec \frac{\pi}{2} =$
- 3.  $\cos \pi =$
- 4.  $\csc\frac{7\pi}{6} =$
- 5.  $\cot 0 =$
- $6. \quad \sin\frac{11\pi}{6} =$
- 7.  $\tan\frac{-3\pi}{4} =$
- 8.  $\cos\frac{7\pi}{3} =$
- 9.  $\cot \frac{\pi}{2} =$
- 10.  $\sin \frac{-3\pi}{2} =$
- 11.  $\sin \frac{19\pi}{6} =$

- NO CALCULATOR
- 12. Evaluate (if possible) the sine, cosine, and tangent of the real number.

$$t = -\frac{3\pi}{4}$$
  
sin t = cos t = tan t =

13. Evaluate (if possible) the sine, cosine, and tangent of the real number.

$$t = \frac{-101\pi}{6}$$

sin t =

tan t =

14. Evaluate (if possible) the sine, cosine, and tangent of the real number.

 $\cos t =$ 

$$t = \frac{205\pi}{2}$$

sin t =

tan t =

15. Evaluate (if possible) the sine, cosine, and tangent of the real number.

 $\cos t =$ 

 $t=150^\circ$ 

 $\sin t = \cos t = \tan t =$ 

**Trig Practice (For Summer Packet)** 

#### Name:

16. Evaluate (if possible) the sine, cosine, and tangent of the real number.

$$t = -60^{\circ}$$

 $\sin t = \cos t = \tan t =$ 

17. Evaluate (if possible) the secant, cotangent, and cosecant of the real number.

$$t = \frac{4\pi}{3}$$

 $\sec t = \cot t = \csc t =$ 

18. Evaluate (if possible) the secant, cotangent, and cosecant of the real number.

$$t = -3\pi$$
  
sec t = cot t = csc t =

19. Given the equation below, determine two solutions such that  $0 \le \theta < 2\pi$ .

$$\tan \theta = \sqrt{3}$$

20. Given the equation below, determine two solutions such that  $0 \le \theta < 2\pi$ .

$$\sin\theta = -\frac{\sqrt{3}}{2}$$

21. Given the equation below, determine two solutions such that  $0 \le \theta < 2\pi$ .  $\csc \theta = 2$ 

- 22. Evaluate  $\arccos \frac{\sqrt{3}}{2}$  without using a calculator.
- 23. Evaluate  $\arcsin \frac{\sqrt{2}}{2}$  without using a calculator.
- 24. Evaluate  $\tan^{-1}\left(-\frac{\sqrt{3}}{3}\right)$  without using a calculator.
- 25. Evaluate  $\sin^{-1}(0)$  without using a calculator.
- 26. Given the equation below, determine two solutions such that  $0 \le \theta < 2\pi$ .

$$\cos\theta = \frac{\sqrt{2}}{2}$$

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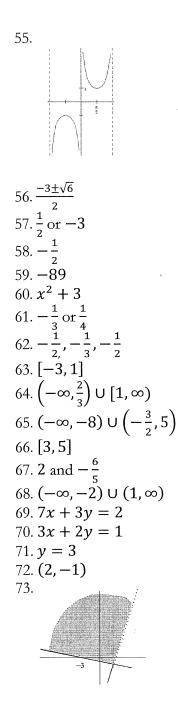
- 27. Find ALL (using correct notation) values of  $\theta$  for which the following is true  $\sin 2\theta = -\frac{1}{2}$
- 28. Find ALL (using correct notation) values of  $\theta$  for which the following is true  $\cos 6\theta = -1$
- 29. Find ALL (using correct notation) values of  $\theta$ for which the following is true  $\tan \frac{\theta}{5} = undefined$

1.  $\frac{x^2+3x}{-1}$ 1.  $\frac{x-4}{x^2-4}$ 2.  $\frac{x-4}{x^2-x}$ 3.  $\frac{5x}{x+5}$  $4. \quad \frac{x+5}{3x+1}$ x 5.  $2(\sqrt{3}-\sqrt{2})$ 6.  $-1 - \sqrt{5}$ 7.  $\frac{1-\sqrt{3}-\sqrt{5}+\sqrt{15}}{1-\sqrt{5}+\sqrt{15}}$ 8.  $8a^{6}b^{-2}$ 9.  $3a^{1/2}b^{3/2}$  $10.\frac{2}{3}a^2b^{-1}$ 11.  $ab^{-1}$ 12.  $a^{-3/2}b$ 13.  $a^{5/6}b^{1/2}$ 14. **1** 15.  $-\frac{3}{2}$ 16.8 17.  $\pm \frac{4}{25}$  $18.\log_2(5(x+1))$ 19. log<sub>2</sub> 3 20. 25  $21.\frac{1}{2}$ 22. **-** *x* 23.  $2 \log_{10} x$  $24. \frac{bcx}{bc-cy-bz}$   $25. \frac{V-2bc}{2(b+c)}$  $26. \frac{A-2\pi r^2}{2}$ 2πr A 27.  $\frac{1}{1+\pi r}$  $28. \frac{\frac{2x-y}{2x-y}}{x+2y}$  $29. \frac{\pi}{\pi-1}$  $30. y + 1 = (x + 2)^2$ 31.  $y - \frac{3}{8} = -\frac{3}{2}\left(x + \frac{1}{2}\right)^2$ 32.  $x + 10 = 9\left(y - \frac{1}{3}\right)^2$ 33.  $x^4(x-4)(x+4)$ 

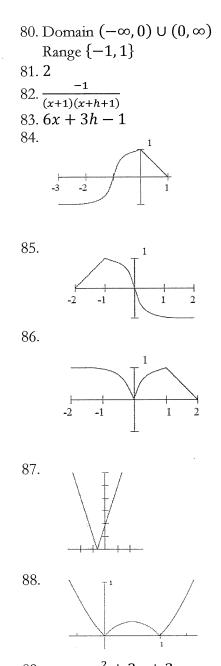
34. (x-2)(2x-5)(2x+5)

35. 
$$(2x + 3)(4x^2 - 6x + 9)$$
  
36.  $(x - 1)(x + 1)(x^2 + 1)$   
37.  $0, \pm 4$   
38.  $2, \pm \frac{5}{2}$   
39.  $-\frac{3}{2}$   
40.  $\frac{\pi}{6}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6}$   
41.  $-\frac{\pi}{2}, \frac{\pi}{6}, \frac{5\pi}{6}$   
42.  $\frac{\pi}{6} + 2k\pi$  and  $\frac{5\pi}{6} + 2k\pi$  where  $k \in I$   
43.  $-\frac{\sqrt{3}}{2}$   
44.  $-\frac{\sqrt{2}}{2}$   
45.  $-\frac{\pi}{4}$   
46.  $-\frac{\pi}{2}$   
47.  $\frac{\sqrt{2}}{2}$   
48.  $\frac{\pi}{3}$   
49.  $\frac{\sqrt{3}}{3}$   
50.  $\frac{3\pi}{4}$   
51.  $\frac{1}{\sqrt{2}}$   
52.  $\frac{1}{\sqrt{2}}$   
53.  $\frac{1}{\sqrt{2}}$   
54.  $\frac{1}{\sqrt{2}}$ 

Answers

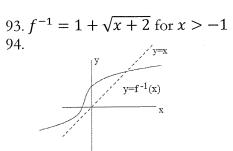


74. 
$$(x - 1)^2 + (y - 2)^2 = 18$$
  
75.  $\left(x - \frac{1}{2}\right)^2 + (y - 1)^2 = \frac{5}{4}$   
76. Center =  $(-3, 2)$ , radius =  $\sqrt{10}$   
77.  $(-\infty, -2) \cup (1, \infty)$   
78. Domain  $(-\infty, \infty)$  Range {7}  
79. Domain  $\left(-\infty, -\frac{1}{2}\right) \cup \left(-\frac{1}{2}, \infty\right)$   
Range  $\left(-\infty, \frac{5}{2}\right) \cup \left(\frac{5}{2}, \infty\right)$ 



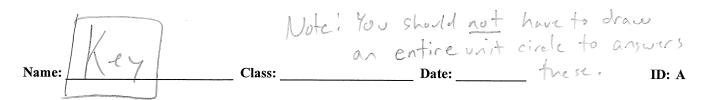
89.  $y = -x^2 + 2x + 3$ 90. 2 1 91.  $f^{-1} = \frac{x-3}{x-3}$ 92

1. 
$$f = \frac{1}{2}$$
  
2.  $f^{-1} = \frac{1}{2}$   
 $\frac{1}{5x-1}$ 



95. 
$$x = t \left(\frac{r-h}{h}\right)$$
  
96. 
$$x = \frac{rt}{\sqrt{r^2 - h^2}}$$
  
97. 
$$1 - \frac{\pi}{4}$$
  
98. 
$$4r + \pi r$$
  
99. 
$$\frac{9\pi}{4}$$

100. 
$$100\sqrt{5} KM$$
  
101.  $\frac{\pi}{6}$   
102.  $2\sqrt{3x-1} - 3$   
103.  $\sqrt{6x-10}$   
104.  $\frac{6x-3}{x}$   
Domain  $(-\infty, 0) \cup (0, \frac{1}{2}) \cup (\frac{1}{2}, \infty)$   
105. Let  $u = 3x$ , then  $y = \sin u$   
106. Let  $u = 2x + 1$ , then  $y = \sqrt[5]{u}$   
107. Let  $u = x^2 - 2x + 5$ ,  
then  $y = u^5$   
108. Let  $u = \cos x$ , then  $y = u^2$ 



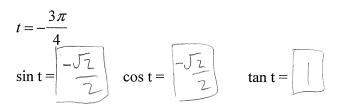


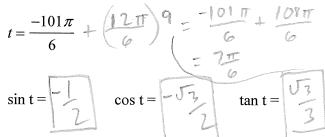
**Trig Practice (For Summer Packet)** 

### NO CALCULATOR

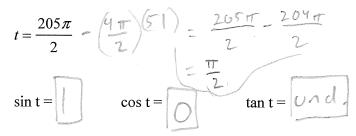
- 1. INSTRUCTIONS: Answer each of the following without a calculator taking no longer than 20 seconds per question. Answers must be exact (no decimals) and radicals need to be simplified/rationalized.
- $\sin \frac{2\pi}{3} = \boxed{\frac{\sqrt{3}}{2}}$ 2.  $\sec \frac{\pi}{2} = \frac{1}{\cos \frac{\pi}{2}} = \frac{1}{\cos \frac{\pi}{2}}$
- 3.  $\cos \pi =$  -
- 4.  $\csc \frac{7\pi}{6} = \frac{1}{\sin 7\pi} = \frac{1}{-\gamma_2} = \frac{1}{-\gamma_2}$ 5.  $\cot 0 = \frac{\cos 0}{\sin 0} = \frac{1}{0} = \text{undefined}$
- 6.  $\sin \frac{11\pi}{6} = \begin{bmatrix} -\frac{1}{2} \end{bmatrix}$
- 7.  $\tan \frac{-3\pi}{4} = \pm \cos \frac{5\pi}{4} = 1$
- 8.  $\cos\frac{7\pi}{3} = \cos\frac{1\pi}{3} = \boxed{2}$
- 9.  $\cot\frac{\pi}{2} = \frac{\cos \pi}{\cos \sqrt{2}} = \frac{0}{1} = 0$
- 10.  $\sin \frac{-3\pi}{2} = \operatorname{Srb} \mathbb{T}_2 = \prod_{n=1}^{\infty} \mathbb{T}_n$
- 11.  $\sin \frac{19\pi}{6} = \sin \frac{7\pi}{6} = -\frac{1}{2}$

12. Evaluate (if possible) the sine, cosine, and tangent of the real number.





14. Evaluate (if possible) the sine, cosine, and tangent of the real number.



15. Evaluate (if possible) the sine, cosine, and tangent of the real number.

$$t = 150^{\circ} = \frac{150}{1} \cdot \frac{17}{140} \text{ rad} = \frac{5\pi}{6} \text{ rad}$$
$$\sin t = \begin{bmatrix} -\frac{1}{2} \\ 2 \end{bmatrix} \quad \cos t = \begin{bmatrix} -\frac{1}{2} \\ 2 \end{bmatrix} \quad \tan t = \begin{bmatrix} -\frac{1}{2} \\ 3 \end{bmatrix}$$



16. Evaluate (if possible) the sine, cosine, and tangent of the real number.

$$t = -60^{\circ}$$

$$\sin t = \begin{bmatrix} -\sqrt{3} \\ 2 \end{bmatrix} \quad \cos t = \begin{bmatrix} 1 \\ 2 \end{bmatrix} \quad \tan t$$

17. Evaluate (if possible) the secant, cotangent, and cosecant of the real number.

$$t = \frac{4\pi}{3} \frac{1}{\frac{1}{\cos^{4}\pi}} \frac{1}{\frac{1}{\cos^{4}\pi}} \frac{1}{\frac{1}{\cos^{4}\pi}} \frac{1}{\frac{1}{\cos^{4}\pi}} \frac{1}{\frac{1}{\cos^{4}\pi}}$$
sec t =  $\boxed{-2}$  cot t =  $\boxed{\sqrt{3}}$  csc t =  $\boxed{\frac{2\sqrt{3}}{3}}$  2

18. Evaluate (if possible) the secant, cotangent, and cosecant of the real number.

$$t = -3\pi = \pi$$
  
sec t =  $\begin{bmatrix} -1 \\ -1 \end{bmatrix}$  cot t =  $\begin{bmatrix} -1 \\ -1 \end{bmatrix}$  csc t =  $\begin{bmatrix} -1 \\ -1 \end{bmatrix}$ 

19. Given the equation below, determine two solutions such that  $0 \le \theta < 2\pi$ .

 $\tan\theta = \sqrt{3} \qquad \boxed{\frac{11}{3}} \neq \boxed{\frac{4}{3}}$ 

20. Given the equation below, determine two solutions such that  $0 \le \theta < 2\pi$ .

21. Given the equation below, determine two solutions such that  $0 \le \theta < 2\pi$ .

$$\csc \theta = 2$$



 $-\frac{1}{2} \leq 0 \leq \frac{1}{2}. \text{ Inverse covint} \mathbf{ID}: \mathbf{A}$  $0 \leq 0 \leq 1 \text{ IT}$ 22. Evaluate  $\arccos \frac{\sqrt{3}}{2}$  without using a calculator.

For 22-25 : Remember invorce sine and inverse tangent have a range

23. Evaluate  $\arcsin\frac{\sqrt{2}}{2}$  without using a calculator.

- 24. Evaluate  $\tan^{-1}\left(-\frac{\sqrt{3}}{3}\right)$  without using a calculator.
  - 5. Evaluate  $\sin^{-1}(0)$  without using a calculator.
- 26. Given the equation below, determine two solutions such that  $0 \le \theta < 2\pi$ .

$$\cos\theta = \frac{\sqrt{2}}{2} \qquad \boxed{1} \qquad \boxed{1} \qquad \boxed{7} \qquad \boxed{7} \qquad \boxed{4} \qquad \boxed{9} \\[9} \[9] \qquad \boxed{9} \\[9} \qquad \boxed{9} \\[9} \\[9] \[9}$$

- 27. Find ALL (using correct notation) values of  $\theta$
- $\begin{cases} \text{for which the following is true } \sin 2\theta = -\frac{1}{2} \\ 2\theta = \frac{11\pi}{6} + 2n\pi \\ 0 = \frac{11\pi}{6} + n\pi \\ 0 = \frac{11\pi}{12} + n\pi \\ 0 = \frac{1$
- 28. Find ALL (using correct notation) values of  $\theta$ for which the following is true  $\cos 6\theta = -1$

$$60 = T + 2nTF$$

$$0 = \frac{1}{6} + \frac{nT}{3}$$

29. Find ALL (using correct notation) values of  $\theta$  $\swarrow$  for which the following is true

$$\tan \frac{\theta}{5} = undefined$$

$$\frac{\Theta}{5} = \frac{\Pi}{2} + n + \Rightarrow \Theta = \frac{5\Pi}{2} + 5n + \frac{1}{2}$$

$$\frac{\Theta}{5} = \frac{1}{2} + n + \frac{1}{2} +$$

AP Calculus Summer Packet Worked-Out Solutions  $\frac{1}{x^{2}-7x+12} = \frac{x(x^{2}-9)}{(x-3)(x-4)} = \frac{x(x-3)(x+3)}{(x-3)(x-4)}$  $= \frac{\chi(x+3)}{\chi-4}$ 

-) X2-2x-8 X3+x2-2x = (x-4)(x+2)  $\overline{X(x^{2}+x-2)}$  $= \frac{(x-y)(x+z)}{x(x+z)(x-1)}$  $= \frac{X-4}{X(X-1)}$ 

Please make note if you think there are any errors in then solutions. We will discuss when we return to school in September.

$$3) \left(\frac{1}{x} - \frac{1}{y_{1}}\right) \left(2^{5}x^{2}\right) = \frac{2^{5}x - 5^{2}x^{2}}{2^{5}x - 5^{2}x^{2}} = \frac{5^{5}x(5 - 4x)}{2^{5}x(5 + x)}$$

$$= \frac{5^{5}x}{5^{5}x(5 + x)}$$

$$= \frac{5^{5}x(5 + x)}{5^{5}x(5 + x)}$$

$$= \frac{5^{$$

11)  $\frac{ab-a}{b^2-b} = \frac{a(b-1)}{b(b-1)} = \frac{a}{b} = \begin{bmatrix} ab^{-1} \end{bmatrix}$  $\frac{12}{(b-1)\sqrt{a}} = \frac{a}{b-1}\frac{1}{a^{2}} = \frac{1}{a^{2}b^{1}}$  $(3)\left(\frac{a}{b^{\frac{1}{2}}}\right)^{2}\left(\frac{b^{\frac{3}{2}}}{a^{\frac{1}{2}}}\right) = \left(\frac{a}{b^{\frac{3}{2}}}\right)\left(\frac{b^{\frac{3}{2}}}{a^{\frac{1}{2}}}\right) = \left(\frac{a}{b^{\frac{3}{2}}}\right)\left(\frac{b^{\frac{3}{2}}}{a^{\frac{1}{2}}}\right) = \left(\frac{a}{b^{\frac{1}{2}}}\right)^{\frac{1}{2}}$ 4) 5(x+1) = 25  $16) \log_{3} x = 3$  $15) \frac{1}{3} = 3^{2r+2}$  $5^{(x+1)} = 5^{2}$  $2^3 = x$ 3-1 = 32++2 X+1 = 2 8=8 X=] -1 = 2x+2-3:2x (7) - 3 = x 1053×2=210924-410935 18) log, 5 + log, (x2-1) - log, (x-1) 1052x2 = 105342 - 10554  $= \log_{2}\left(\frac{5(x^{2}-1)}{x-1}\right) = \log_{2}\left(\frac{5(x-1)(x+1)}{(x-1)}\right)$ 1093×2 = 1093(42)  $= \left| \log_{2}(f(x+1)) \right|$  $\chi^2 = \frac{4^2}{5^4}$ 19) 2 logy 9 - log, 3 of base formula  $\left[\chi = \frac{\pm 4}{25}\right]$  $=2\left(\frac{\log_2 9}{\log_2 9}\right) - \log_2 3$ 105,4=2 = 10929 - 10923 b/c 22=4 = log (==) = [log 2]

20) 3210935 = 3109352 = 52= 25 21)  $\log_{10} 10^{\frac{1}{2}} = \frac{1}{2}$  22)  $\log_{10} (10^{\frac{1}{2}}) = \log_{10} 10^{-\frac{1}{2}} = \frac{1}{2}$ 24) ~+ + + == | 23) 2 log , Jx + 3 log , x 3 X=1-7-=  $\log (\sqrt{x})^2 + \log (x^{\frac{1}{3}})^{\frac{1}{2}}$  $\chi = \alpha \left(1 - \frac{\gamma}{6} - \frac{z}{c}\right)$ 10510 × + 10510 ×  $\frac{\lambda}{1-\frac{1}{2}-\frac{1}{2}} = \alpha$ log10x2 = 210910x  $\frac{xbc}{bc-cy-bz} = a$ 25) V= 2 (ab + bc + ca)  $\frac{V}{7}$  = ab + bc + ca  $26)A = 2\pi r^2 + 2\pi rh$  $\frac{U}{2}$  - bc = ab + ca A - 2112 = 21114  $\frac{V}{2} - bc = a(btc)$ A-2+12=h 200  $\frac{V}{2(btc)} - \frac{bc}{(btc)} = a$ 28) 2x - 2y d= y+xd  $(27)A = P + \pi r P$ 2x-y = 2yd + xd  $A = P(1+\pi r)$ 2x - y = d(2y + x). $\frac{V-2bc}{2(b+q)} = a$  $\frac{A}{1+nr} = P$  $\frac{2x-y}{2y+x} = d$ 和美国的基本公司和中国法院的专家和学校 4.1

30)  $\gamma = x^2 + 4x + 3$  $\frac{29}{4\pi}\left(\frac{2x}{4\pi} + \frac{1-x}{2}\right) = 6 + 4\pi$  $\gamma = (x^2 + 4x + 4) + 3 - 4$  $2x + 2\pi - 2\pi x = 0$  $y = (x+2)^2 - 1$ X + T - TX=0  $[y+1 = (x+2)^2]$ T = T X - XT= ×(T-1) 31)  $3x^2 + 3x + 2y = 0$  $\begin{bmatrix} T \\ T \\ T - 1 \end{bmatrix} = X$  $3x^2+3x = -2y$  $32)_{q}^{2}(9_{y}^{2} - 6_{y} - 9 - x) = (0)_{q}^{2}$  $\binom{2}{1}(x+\frac{1}{2})^{2}=(-\frac{2}{5}\gamma+\frac{1}{4})^{-\frac{2}{2}}$ y2 - 2y - 1 - 1x = 0  $\left| -\frac{3}{2} \left( x + \frac{1}{2} \right)^2 = \gamma - \frac{3}{8} \right|$  $y^2 - \frac{2}{3}y = \frac{1}{9}x + 1$  $y^{2} - \frac{1}{5}y + \frac{1}{9} = \frac{1}{9}x + |+\frac{1}{9}|$ 36) 33) × 6-16×4 x4-1  $q\left(\left(\gamma-\frac{1}{3}\right)^{2}\right)=\left(\frac{1}{9}\times+\frac{10}{9}\right)q$ (x2-1) (x2+1) x4(x2-16)  $\left| 9(y-5)^2 = x+10 \right|$ (x-1)(x+1)(x+1) (x4 (x-4) (x+4) 37) ×4 (x-4)(x+4)=0 34) 4x3-8x2-25x+50 x=0 x=4 x=-4 4x2(x-2)-25(x+2) 35)  $8x^3 + 27 = (2x)^3 + (3)^3$ ) (4×2-25)(×-2) =[(2x+3)(4x<sup>2</sup>-6x+9)] (2x-5)(2x+5)(x-2)=0 $\frac{R_{u}(c)}{a^{3}+b^{3}} = (a+b)(a^{2}-ab+b^{2})$ TX= 5 x=-5 x=2 a3-67 = (a-b) (a2+ab+b2)

$$39)(2x+3)(4x^{2}-(x+9)=0$$

$$2x+3=0$$

$$4x^{2}-6x+1=0$$

$$2x-3$$

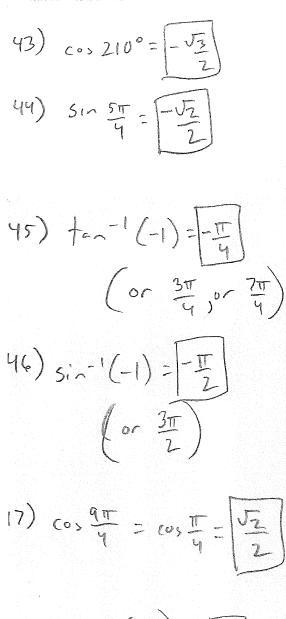
$$yo Re-1 soldiers
$$\frac{1}{|x|^{2}-\frac{3}{2}|}$$

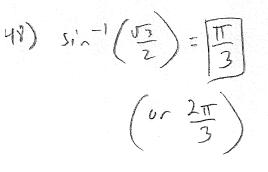
$$y = sin^{2}x = sin^{2}x$$

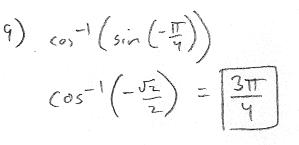
$$y = sin^{2}x = \frac{1}{2}$$

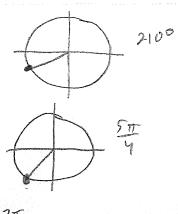
$$y = \frac{1}{|x|^{2}-\frac{3}{2}|}$$

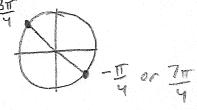
$$y = \frac{1}{|x|^{2}-\frac{3}{2}|}$$$$$$$$$$$$$$$$$$$$$$$$$$$$$$$$$$

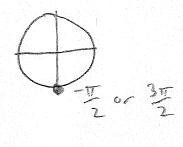


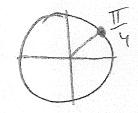


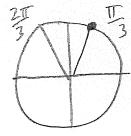




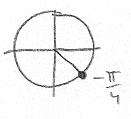


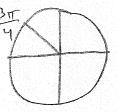






 $\sin \frac{-\pi}{4} = \frac{-\pi}{2}$  $\left(\circ s^{-1}\left(\frac{-\sqrt{L}}{L}\right)\right)$ 





$$51-5^{\circ} = 51 + 52^{\circ} + 12 + 3 = 0$$

$$x = \frac{-12 \pm J(1+1) - 4V}{2(1+1)}$$

$$x = \frac{-12 \pm J(1+1) - 4V}{2(1+1)}$$

$$x = \frac{-12 \pm J(1+1) - 4V}{8}$$

$$x = \frac{-12 \pm J(1+$$

$$(60) \times 3 + 0 \times 2 + 0 \times 10^{-10}$$

 $\frac{1}{2}$ 

+|

$$\frac{\chi^{2} - \chi + 1 + \frac{\chi^{2} + 3}{\chi^{3} + 1}}{[\chi^{5} - \chi^{4} + \chi^{3} + 2\chi^{2} - \chi + 4]}$$

$$-\chi^{5} = 0 = -\chi^{4} + \chi^{3} + \chi^{2} - \chi$$

$$-\chi^{4} + \chi^{3} + \chi^{2} - \chi$$

$$+\chi^{4} = 0 = 0 + \chi$$

$$-\chi^{4} = 0 = 0 + \chi$$

$$-\chi^{3} = 0 + \chi$$

$$-\chi^{3} = 0 = 0 + \chi$$

$$-\chi^{3} = 0 = 0 + \chi$$

$$-\chi^{3} = 0 = 0 + \chi$$

 $\frac{-12}{4-3}$ 

$$2 \begin{vmatrix} 12 & -23 & -3 & 2 \\ 24 & 2 & -2 \\ 12 & 1 & -1 & 10 \end{vmatrix}$$

$$|2x^{2} + |x - | = 0$$
  

$$|2x^{2} + |x - | = 0$$
  

$$|2x^{2} + |x - 3x - | = 0$$
  

$$|4x(3x+1) - |(3x+1) = 0$$
  

$$(4x-1)(3x+1) = 0$$

$$4x - 1 = 0$$
  
 $4x = 1$   
 $5x = -1$   
 $5x = -1$ 

$$\begin{array}{c} (5) \quad \underbrace{Crdicl (hdurs)}_{X=Y=2} & 2x+3=0 \\ 2x=-3 \\ x=-\frac{2}{2} \\ \end{array} \quad \begin{array}{c} x=r \\ z=r \\ y=-\frac{2}{2} \\ \end{array} \quad \begin{array}{c} x=r \\ 2x+3=\frac{2}{x-r} \\ z=r \\ y=x \\ \hline \\ -y=x \\ \hline \\ \hline \\ (-\infty,-2) \cup (-\frac{2}{x},5) \\ \hline \\ (-\infty,-2) \cup (1,\infty) \\ y=x \\ \hline \\ (-\infty,-2) \cup (1,\infty) \\ \hline \\ (-\infty,-2) \cup (1,\infty) \\ y=x \\ \hline \\ (-\infty,-2) \cup (1,\infty) \\ \hline \\ (-\infty,-2) \cup (1,\infty) \\ \hline \\ (-\infty,-2) \cup (1,\infty) \\ y=x \\ \hline \\ (-\infty,-2) \cup (1,\infty) \\ y=x \\ \hline \\ (-\infty,-2) \cup (1,\infty) \\ y=x \\ \hline \\ (-\infty,-2) \cup (1,\infty) \\ \hline \\ (-\infty,-2) \hline$$

$$71) \text{ Midpoint!} \begin{pmatrix} -1+3 & 4i1\\ 2 & 72 \end{pmatrix} \Rightarrow \begin{pmatrix} 1,3 \end{pmatrix}$$

$$m = \frac{3-3}{1-2} = 0 \qquad y-3 = 0(x-2)$$

$$y = 3$$

$$72) 5(3x - y - 7 = 0) \qquad 15x - 5x - 0 \qquad \text{Morin}$$

$$x + 5y + 3 = 0 \qquad x + 5y + 5 = 0$$

$$x + 5y + 3 = 0 \qquad x + 5y + 5 = 0$$

$$y = 32 \qquad y^{2-1}$$

$$y = -3 \qquad y^{2-1}$$

$$(x - 1)^{2} + (y - 1)^{2}$$

76) Rearrance and complete the square  

$$x^{2} + y^{2} + 6x - 4y + 3 = 0$$

$$x^{2} + 6x + 9 + y^{2} - 4y + 9 = -3 + 9 + 9$$

$$(x + 3)^{2} + (y - 2)^{2} = 10$$

$$(x + 3)^{2} + (y - 2)^{2} = 10$$

$$(x + 1)(x + 2)$$

$$y = x^{2} + x - 2 > 0$$

$$y = x^{2} + x - 2 > 0$$

$$y = x^{2} + x - 2 > 0$$

$$y = x^{2} + x - 2 > 0$$

$$y = x^{2} + x - 2 > 0$$

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$$y = x^{2} + x - 2 > 0$$

$$y = x^{2} + x - 2 > 0$$

$$y = x^{2} + x - 2 > 0$$

$$y = x^{2} + x^{2}$$

$$81) \underbrace{\begin{pmatrix} 1 \\ (h+1)+1 \\ (h) \end{pmatrix}}_{(h)} (x+1)(x+1) = \frac{x+1(-x-h-2)}{h(x+1+1)(x+1)} = \frac{-h}{h(x+1+1)(x+1)}$$

$$= \frac{x+1-(x+h+1)}{h(x+1+1)(x+1)} = \frac{x+1(-x-h-2)}{h(x+1+1)(x+1)} = \frac{-h}{h(x+1+1)(x+1)}$$

$$= \frac{-1}{(x+h+1)(x+1)}$$

$$K = \frac{-1}{(x+h+1)(x+1)}$$

$$= \frac{-1}{(x+h+1)(x+1)}$$

$$=$$

93) 
$$y = x^2 - 2x - 1$$
  
 $x = y^2 - 2y - 1$   
 $x = y^2 - 2y - 1$   
 $x + 1 = y^2 - 2y$   
 $x + 1 + 1 = y^2 - 2y + 1$   
 $x + 2 = (y - 1)^2$   
 $(y + 1 = y)$   
 $(y + 1$ 

$$\begin{array}{l} 102) f(s(r)) = \overline{2\sqrt{3r-1} - 3} \\ 104) f(s(r)) = \overline{\frac{3}{(\frac{x}{2r-1})}} \\ 103) g(f(r)) = \sqrt{3(2r-3) - 1} \\ = \sqrt{6r-9 - 1} \\ = \overline{\sqrt{6r-9 - 1}} \\ = \overline{\sqrt{6r-10}} \\ \hline 0: (-\infty, 0) \cup (0, \frac{1}{2}) \cup (\frac{1}{2}, \infty) \end{array}$$

105 - 108: See other animers